Last time: Gaussian Elim Solution Paradigms A linear System has 3 possible soltion paradigns: -> No solutions * (from an inconsistent equation) -> Exactly 1 Solition * -> Infinitely many solutions <- X The These are the only three possibilities... Goal: Determine Solution Sets. Crave Soldins as Glum vectors. In general we give a full set of Column vectors Ex: Last the ne solved $\begin{cases} 2 \times & + 2 + h = 5 \\ 3 \times & -2 - h = 0 \\ 4 \times & + y + 22 + w = 9 \end{cases} \qquad \begin{cases} x = 0 \\ y = -1 + t \\ 7 = 5 - t \end{cases} \qquad \begin{cases} x = 0 \\ y = -1 + t \\ 7 = 5 - t \end{cases} \qquad \begin{cases} x = 0 \\ y = -1 + t \\ 7 = 5 - t \end{cases} \qquad \begin{cases} x = 0 \\ y = -1 + t \\ 7 = 5 - t \end{cases} \qquad \begin{cases} x = 0 \\ y = -1 + t \\ 7 = 5 - t \end{cases} \qquad \begin{cases} x = 0 \\ y = -1 + t \\ 7 = 5 - t \end{cases} \qquad \begin{cases} x = 0 \\ y = -1 + t \\ y = -1 + t \end{cases} \qquad \begin{cases} x = 0 \\ y = -1 + t \\ y = -1 + t \end{cases} \qquad \begin{cases} x = 0 \\ y = -1 + t \\ y = -1 + t \end{cases} \qquad \begin{cases} x = 0 \end{cases} \qquad \begin{cases} x = 0 \\ y = -1 + t \end{cases} \qquad \begin{cases} x = 0 \end{cases} \qquad \begin{cases} x = 0 \end{cases} \qquad \begin{cases} x = 0 \\ y = -1 + t \end{cases} \qquad \begin{cases} x = 0 \end{cases}$ we write the solution set like so: $\begin{vmatrix} 0 & 1 & 1 \\ -1 & 1 & 1 \\ 5 & -1 & 1 \end{vmatrix} = \begin{bmatrix} 0 \\ -1 \\ 5 \\ 0 \end{bmatrix} + \begin{bmatrix} 0 \\ 1 \\ -1 \\ 1 \end{bmatrix} = \begin{bmatrix} 0 \\ -1 \\ 5 \\ 0 \end{bmatrix} + 1 \begin{bmatrix} 0 \\$ MB: this vector is a particular solution.

Matrices

A matrix is a rectangular array of numbers

 $\begin{bmatrix} 2 & 2 \\ 1 & 5 \\ 1 & -1 \end{bmatrix}$ $\begin{bmatrix} 3 & 2 \\ 1 & 0 \end{bmatrix}$ 2×2

[0 0 5]

An mxn matrix has m rows an u columns

A column vector is an NXI matrix.

A von vector is a IXN matrix.

The entries of a matrix are the numbers in the notion Entries are indexed by row and column.

Ex: $A = \begin{bmatrix} 0 & 1 & -1 & 2 & 5 \\ 1 & 0 & -3 & 0 & 2 \\ 0 & -7 & \pi & e & Y \end{bmatrix}$ Column

Number

Number

Convention: Matrices are represented of Capital letters.

the corresponding entries are repid by the lowerese letter, so $D = \int d_{i,j}$.

We can represent a linear system via an arguented matrix.

 $Ex: \begin{cases} 3x + 59 - 72 + w = 0 \\ 59 - 32 + v = 5 \\ x - 2 = 6 \end{cases} \begin{bmatrix} 3 & 5 - 7 & 1 & 0 \\ 0 & 5 & -3 & 1 & 5 \\ 1 & 0 & -1 & 0 & 6 \end{bmatrix}$

Let's solve this system u/ its matrix representation

translates into "ron operations" NB: Gaussian elimination for the matrix setup. $\frac{\beta_{3}-3\beta_{1}}{0} = \begin{bmatrix}
1 & 0 & -1 & 0 & | & 6 \\
0 & 5 & -3 & 1 & | & 5 \\
0 & 5 & -4 & 1 & | & -18
\end{bmatrix}$ $\frac{\beta_{3}-\beta_{2}}{0} = \begin{bmatrix}
1 & 0 & -1 & 0 & | & 6 \\
0 & 5 & -3 & 1 & | & 5 \\
0 & 0 & -1 & 0 & | & -23
\end{bmatrix}$ (lence he has solution set $\begin{cases} 29 \\ 74 \\ 5 \\ 23 \end{cases}$: $t \in \mathbb{R}$ OR $\begin{cases} 29 \\ 0 \\ 23 \\ 741 \end{cases} + S \begin{bmatrix} 0 \\ 0 \\ -5 \end{bmatrix}$: SEIR \end{cases} Some solution Set, \boxed{A}

Ex: Solve
$$\begin{cases} x_1 - x_2 + 2x_3 = 4 \\ x_1 - x_2 + 5x_3 = 17 \end{cases}$$

Sol: $\begin{cases} 0 & 0 & 1 & 4 \\ 1 & -1 & 2 & 5 \\ 1 & 7 & 7 \end{cases}$
 $\begin{cases} x_1 - 1 & 2 & 4 \\ 2 & -1 & 5 & 7 \end{cases}$
 $\begin{cases} x_1 - 1 & 2 & 4 \\ 3 & 7 & 7 \end{cases}$
 $\begin{cases} x_1 - 1 & 2 & 4 \\ 4 & -1 & 5 & 7 \end{cases}$
 $\begin{cases} x_1 - 1 & 2 & 4 \\ 5 & 7 & 7 \end{cases}$
 $\begin{cases} x_1 - 1 & 2 & 4 \\ 2 & 7 & 7 \end{cases}$
 $\begin{cases} x_1 - 1 & 2 & 4 \\ 2 & 7 & 7 \end{cases}$
 $\begin{cases} x_1 - 1 & 2 & 4 \\ 2 & 7 & 7 \end{cases}$
 $\begin{cases} x_1 - 1 & 2 & 4 \\ 2 & 7 & 7 \end{cases}$
 $\begin{cases} x_1 - 2 & 2 & 4 \\ 2 & 7 & 7 \end{cases}$
 $\begin{cases} x_1 - 2 & 2 & 7 \\ 2 & 7 & 7 \end{cases}$
 $\begin{cases} x_1 - 2 & 2 & 7 \\ 2 & 7 & 7 \end{cases}$
 $\begin{cases} x_1 - 2 & 2 & 7 \\ 2 & 7 & 7 \end{cases}$
 $\begin{cases} x_1 - 2 & 2 & 7 \\ 2 & 7 & 7 \end{cases}$
 $\begin{cases} x_1 - 2 & 2 & 7 \\ 2 & 7 & 7 \end{cases}$
 $\begin{cases} x_1 - 2 & 2 & 7 \\ 2 & 7 & 7 \end{cases}$
 $\begin{cases} x_1 - 2 & 2 & 7 \\ 2 & 7 & 7 \end{cases}$
 $\begin{cases} x_1 - 2 & 2 & 7 \\ 2 & 7 & 7 \end{cases}$
 $\begin{cases} x_1 - 2 & 2 & 7 \\ 2 & 7 & 7 \end{cases}$
 $\begin{cases} x_1 - 2 & 2 & 7 \\ 2 & 7 & 7 \end{cases}$
 $\begin{cases} x_1 - 2 & 2 & 7 \\ 2 & 7 & 7 \end{cases}$
 $\begin{cases} x_1 - 2 & 2 & 7 \\ 2 & 7 & 7 \end{cases}$
 $\begin{cases} x_1 - 2 & 2 & 7 \\ 2 & 7 & 7 \end{cases}$
 $\begin{cases} x_1 - 2 & 2 & 7 \\ 2 & 7 & 7 \end{cases}$
 $\begin{cases} x_1 - 2 & 2 & 7 \\ 2 & 7 & 7 \end{cases}$
 $\begin{cases} x_1 - 2 & 2 & 7 \\ 2 & 7 & 7 \end{cases}$
 $\begin{cases} x_1 - 2 & 2 & 7 \\ 2 & 7 & 7 \end{cases}$
 $\begin{cases} x_1 - 2 & 2 & 7 \\ 2 & 7 & 7 \end{cases}$
 $\begin{cases} x_1 - 2 & 2 & 7 \\ 2 & 7 & 7 \end{cases}$
 $\begin{cases} x_1 - 2 & 2 & 7 \\ 2 & 7 & 7 \end{cases}$
 $\begin{cases} x_1 - 2 & 2 & 7 \\ 2 & 7 & 7 \end{cases}$
 $\begin{cases} x_1 - 2 & 2 & 7 \\ 2 & 7 & 7 \end{cases}$
 $\begin{cases} x_1 - 2 & 2 & 7 \\ 2 & 7 & 7 \end{cases}$
 $\begin{cases} x_1 - 2 & 2 & 7 \\ 2 & 7 & 7 \end{cases}$
 $\begin{cases} x_1 - 2 & 2 & 7 \\ 2 & 7 & 7 \end{cases}$
 $\begin{cases} x_1 - 2 & 2 & 7 \\ 2 & 7 & 7 \end{cases}$
 $\begin{cases} x_1 - 2 & 2 & 7 \\ 2 & 7 & 7 \end{cases}$
 $\begin{cases} x_1 - 2 & 2 & 7 \\ 2 & 7 & 7 \end{cases}$
 $\begin{cases} x_1 - 2 & 2 & 7 \\ 2 & 7 & 7 \end{cases}$
 $\begin{cases} x_1 - 2 & 2 & 7 \\ 2 & 7 & 7 \end{cases}$
 $\begin{cases} x_1 - 2 & 2 & 7 \\ 2 & 7 & 7 \end{cases}$
 $\begin{cases} x_1 - 2 & 2 & 7 \\ 2 & 7 & 7 \end{cases}$
 $\begin{cases} x_1 - 2 & 2 & 7 \\ 2 & 7 & 7 \end{cases}$
 $\begin{cases} x_1 - 2 & 2 & 7 \\ 2 & 7 & 7 \end{cases}$
 $\begin{cases} x_1 - 2 & 2 & 7 \\ 2 & 7 & 7 \end{cases}$
 $\begin{cases} x_1 - 2 & 2 & 7 \\ 2 & 7 & 7 \end{cases}$
 $\begin{cases} x_1 - 2 & 2 & 7 \\ 2 & 7 & 7 \end{cases}$
 $\begin{cases} x_1 - 2 & 2 & 7 \\ 2 & 7 & 7 \end{cases}$
 $\begin{cases} x_1 - 2 & 2 & 7 \\ 2 & 7 & 7 \end{cases}$
 $\begin{cases} x_1 - 2 & 2 & 7 \\ 2 & 7 & 7 \end{cases}$
 $\begin{cases} x_1 - 2 & 2 & 7 \\ 2 & 7 & 7 \end{cases}$
 $\begin{cases} x_1 - 2 & 2 & 7 \\ 2 & 7 & 7 \end{cases}$
 $\begin{cases} x_1 - 2 & 2 & 7 \\ 2 & 7 & 7 \end{cases}$
 $\begin{cases} x_1 - 2 & 2 & 7 \\ 2 & 7 & 7 \end{cases}$
 $\begin{cases} x_1 - 2 & 2 & 7 \\ 2 & 7 \end{cases}$
 $\begin{cases} x_1 - 2 & 2 & 7 \\ 2 & 7 & 7 \end{cases}$

Sol:
$$\begin{bmatrix} 3 & 2 & 5 \\ -6 & -4 & 0 \end{bmatrix} \xrightarrow{(2+21)} \begin{bmatrix} 3 & 2 & 5 \\ 0 & 0 & 10 \end{bmatrix} \angle$$

.: 0=10 is implied by the second row,

So the solution set is
$$\emptyset = \{3\}$$

Lemply set.

Preview of Coming Attactions: Matrix Algebra. Operations on natrices (today): -> Normal row operations (sup, all, notiphy). Defn: Let A and B be nown matrices
and let c ER be constant.

The Sum of A and B is $A+B = \begin{bmatrix} a_{i,1}+b_{i,j} \end{bmatrix}$, i.e. the matrix obtained by entry-wise addition.

The Scalar multiple of A by (is $A = \begin{bmatrix} ca_{i,j} \end{bmatrix}$), the matrix obtained from an Hiphynny each entry of A by C.

Ex: $\begin{bmatrix} 3 & -1 & 0 \\ 2 & 0 & 1 \end{bmatrix} + \begin{bmatrix} 7 & -1 & 0 \\ 0 & -1 & -1 \end{bmatrix} = \begin{bmatrix} 3+1 & -1-1 & 0+0 \\ 2+0 & 0-1 & 1-1 \end{bmatrix} = \begin{bmatrix} 10 & 2 & 0 \\ 2+0 & 0-1 & 1-1 \end{bmatrix}$ S $\begin{bmatrix} 2 & 3 \\ 1 & 3 \end{bmatrix} = \begin{bmatrix} 5 & 2 & 5 & 3 \\ 5 & 1 & 5 & -3 \end{bmatrix} = \begin{bmatrix} 10 & 15 \\ 5 & -15 \end{bmatrix}$ Non-ex: $\begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 5 \end{bmatrix} + \begin{bmatrix} 3 & 0 \\ 0 & 3 & 7 & -2 \end{bmatrix}$ TS UND FINED!